

Properties of the Gamma Function

$$\Gamma(1 + n) = n!$$

$$\Gamma(1 + z) = z\Gamma(z)$$

$$\Gamma^*(z) = \Gamma(z^*)$$

$$\Gamma\left(\frac{1}{2}\right) = \sqrt{\pi}$$

$$\Gamma(z)\Gamma(1 - z) = \frac{\pi}{\sin \pi z}$$

$$\Gamma\left(\frac{1}{2} + z\right)\Gamma\left(\frac{1}{2} - z\right) = \frac{\pi}{\cos \pi z}$$

$$\Gamma(z)\Gamma\left(z + \frac{1}{2}\right) = \sqrt{2\pi} 2^{-2z + \frac{1}{2}} \Gamma(2z)$$