

COMPLEX ELECTRIC DIPOLES

Consider a set of charges, each of magnitude $q = 4 \epsilon_0 d^2 E_0$.

a. Use Maple to plot the resulting electric fields in the region

$$-10d < x < 10d, \quad -10d < y < 10d, \quad -10d < z < 10d,$$

when the positions of the charges are as follows:

- i. one charge $+q$ at $z = 0.9d, x = y = 0$
- ii. like i plus another charge $-q$ at $z = -0.9d, x = y = 0$
- iii. like ii plus another pair of charges $\pm q$ at $y = \pm 0.9d, x = z = 0$

0

- iv. like ii plus another pair of charges:
 $+q$ at $z = -0.9d, y = +0.6d, x = 0$
 $-q$ at $z = +0.9d, y = +0.6d, x = 0$

b. For each case, multiply the resulting field by an appropriate power of $r = \sqrt{x^2 + y^2 + z^2}$ so that, at large r , the magnitude of the field vectors becomes independent of r . For each case, plot the modified field.

Be sure to give the power of r .

c. For each charge distribution, what is the direction and magnitude of the dipole moment \mathbf{p} ?

Your solution to this exercise should include

- Maple output (eight 3-dimensional vector graphs)
- the input for each graph
- for each case i-iv, the dipole moment and the power law